

Harvard School of Engineering and Applied Sciences — CS 152: Programming Languages
Logic Programming; Dynamic Types; Probabilistic Programming
Section and Practice Problems

April 20– April 24, 2020

1 Logic Programming

To try playing around with Prolog, go to <http://www.swi-prolog.org/>. You will be able to use Prolog online at <https://swish.swi-prolog.org/>.

To try playing around with Datalog, you can go to either <http://abcdatalog.seas.harvard.edu/> to download a Java-based Datalog implementation, or you can go to <https://datalog.db.in.tum.de/> to use Datalog online.

Although you can use the tools above to get the answers to the section problems below very easily, work out the answers by hand (to make sure you understand the semantics of Prolog and Datalog), and then you can check your answers by using the tools to execute the programs.

- (a) Consider the following Prolog program (where $[]$ is a constant representing the empty list, $[t]$ is shorthand for $\text{cons}(t, [])$ and $[t_1, t_2|t_3]$ is shorthand for $\text{cons}(t_1, \text{cons}(t_2, t_3))$).

```
foo([], []).  
foo([X], [X]).  
foo([X, Y|S], [Y, X|T]) :- foo(S, T).
```

For each of the following queries, compute the substitutions that Prolog will generate, if any. (Note that there is a difference between an empty substitution, and no substitution.) If the query evaluation will not terminate, explain why.

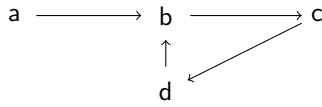
- $\text{foo}([a, b], X)$.
- $\text{foo}([a, b, c], X)$.
- $\text{foo}([a, b], [a, b])$
- $\text{foo}(X, [a])$
- $\text{foo}(X, Y)$.

- (b) Consider the following Datalog program.

```
bar(a, b, c).  
bar(X, Y, Z) :- bar(Y, X, Z).  
bar(X, Y, Z) :- bar(Z, Y, X), quux(X, Z).  
quux(b, c).  
quux(c, d).  
quux(X, Y) :- quux(Y, X).  
quux(X, Z) :- quux(X, Y), quux(Y, Z).
```

Find all solutions to the query $\text{bar}(X, Y, Z)$.

- (c) Suppose that we represent a directed graph using the predicates $\text{edge}(X, Y)$ to indicate that there is an edge from node X to node Y . For example, the following graph is represented by the following facts:



node(a).
 node(b).
 node(c).
 node(d).
 edge(a, b).
 edge(b, c).
 edge(c, d).
 edge(d, b).

- (i) Write a Datalog program that computes $\text{reachable}(X, Y)$, where $\text{reachable}(X, Y)$ holds if there is a path (of zero or more edges) from X to Y .
- (ii) Write a Datalog program that computes $\text{sameSCC}(X, Y)$, where $\text{sameSCC}(X, Y)$ holds if nodes X and node Y are in the same strongly connected component. (Hint: use the predicate reachable .)

2 Dynamic types and contracts

- (a) To make sure you understand the operational semantics of dynamic types and exceptions, show the execution of the following program under the semantics of Section 1 of the Lecture 25 notes.

```
let f = λx. 42 + x in
let g = λy. (y true) + 42 in
g f
```

- (b) Modify the program from question (a) by adding appropriate error handlers (i.e., expressions of the form $\text{try } e_1 \text{ catch } x. e_2$ to catch the type error and return the integer 42 as the final result of the program. There are multiple places in the program where you can insert an error handler to achieve the desired result. Show three variations and their executions. (Note that the semantics for the execution of your programs is from Part 2 (Exception handling) of the Lecture 22 notes.)
- (c) Modify the program from question (a) by adding appropriate dynamic type checks to raise the error as early as possible. When does your program detect the error?
- (d) Modify the program from question (a) by adding contracts that specify the types of the input and output of f and g . Show the execution of the modified program.

3 Probabilistic Programming

- (a) Consider the following Bayesian Network for enrollment in intro level CS courses:

$$\text{CS50} \mid \begin{array}{l} \top \\ 0.5 \end{array} \mid \begin{array}{l} \perp \\ 0.5 \end{array}$$

$$\begin{array}{l} \text{CS50} \\ \top \\ \perp \end{array} \mid \begin{array}{l} \text{CS51} \\ 0.6 \\ 0.05 \end{array} \mid \begin{array}{l} \text{!CS51} \\ 0.4 \\ 0.95 \end{array}$$

What is the probability that someone takes CS51 given that they took CS50?

- (b) What is the probability that someone takes CS51 given that they took CS50?

CS50	CS51	CS61	!CS61
T	T	0.5	0.5
T	⊥	0.4	0.6
⊥	T	0.95	0.05
⊥	⊥	0.01	0.99

- (c) What is the probability that someone has taken CS50 given that they took CS61?
- (d) You want to use probabilistic programming for your new favorite hobby: bird watching! You live in a great area for birding, so you decide to run a linear regression on the correlation between the number of birds and the time of day. What is your output (or data) for the probabilistic program and what are your parameters?
- (e) Your linear regression didn't work you had hoped it would, but you've moved on to a bigger question: where should birds land to find a worm? Say that birds land in a two dimensional field. What is the data you give your program and what are the parameters you hope to find?