

## ES50 Problem Set

1. Simplify the following function using K map and the don't care states d: then express the simplified function as a sum of min terms:  
$$F(x, y, z) = \Sigma(0, 1, 2, 4, 5)$$
$$d(x, y, z) = \Sigma(3, 6, 7)$$
2. Simplify the following function using K map and the don't care states d: then express the function as both a sum of products and a product of sums;  
$$F(w, x, y, z) = \Sigma(0, 1, 2, 3, 7, 8, 10)$$
$$d(w, x, y, z) = \Sigma(5, 6, 11, 15)$$
3. A logic circuit implements the following function:  
$$F = A'C + AC'D'$$

It is found that the input combination  $A = C = 1$  can never occur. Find a simpler expression for  $F$  using the proper don't care conditions.
4. Complete the design started in class for a BCD to decimal decoder making use of don't care states, if any, to simplify the logic.
5. A combinational circuit is defined by the following three functions. Design the circuit using a decoder and external gates:  
$$F1 = x'y'z' + xz$$
$$F2 = xy'z' + x'y$$
$$F3 = x'y'z + xy$$
6. A combinational circuit is defined by the following functions. Design the circuit using a decoder and minimal external logic:  
$$F1 = \Sigma(2, 4, 7)$$
$$F2 = \Sigma(0, 3)$$
$$F3 = \Sigma(0, 2, 3, 4, 7)$$
7. Construct a 5x32 decoder using four 3x8 decoders with enable and one 2x4 decoder. Use block diagrams.
8. Implement the following function with an 8x1 MUX:  
$$F(A, B, C, D) = \Sigma(0, 3, 5, 6, 8, 9, 14, 15)$$
9. An 8x1 MUX has inputs A, B, and C connected to the select inputs  $s_2, s_1,$  and  $s_0$  respectively. The data inputs  $D_0$  through  $D_7$  are as follows;  $D_1 = D_2 = D_7 = 0$ ;  $D_3 = D_5 = 1$ ;  $D_0 = D_4 = D$ ; and  $D_6 = D'$ . Determine the function that the MUX implements.
10. Implement the following function using a 4x1 MUX and external logic:  
$$F(A, B, C, D) = \Sigma(1, 3, 4, 11, 12, 13, 14, 15)$$