

**Figure 2** MOC image showing blanketing material filling several craters that are 200–400 m in diameter. Image scale, 4.1 by 7.3 m per pixel; 3.6° S, 340.5° W. The crater rims are moderately well preserved and visible, indicating that aeolian material has not simply been draped over the topography but has preferentially filled the lowest areas. The average depth of fresh 200-m craters is probably ~20 m. Rim heights above surroundings are typically much less than crater depths; thus the fill inside these craters is probably deeper than in much of the intervening plains.

crater in  $10^6$  yr, but the clear lesson from the MOC data is that the blankets are not uniformly distributed airfall but represent a net sum of airfall, erosion, saltation cleaning and deposition. Other small craters have fill with periodic bedforms, and erosional stripping of layers and jointed sediments. The ubiquity of martian aeolian material is emphasized by the filling of craters and structural features high on Arsia Mons, more than 20 km above the reference 6.1-mbar level in the atmosphere; these deposits indicate transport of considerable amounts of material at pressures under 1 mbar (ref. 29; unless there has been a geologically recent period of higher atmospheric pressure on Mars, which is generally considered very unlikely<sup>21</sup>).

The indications of distinctive materials, possibly sulphates, moved in saltation on Mars expands the known complexity of the martian sedimentary system, and implies that remnants of ancient sedimentary and weathering processes have not been completely homogenized and lost from remote or *in situ* studies. This variety may assist some future sampling efforts, but the presence of widespread mantling reduces the areas within which bedrock or sorted remnants are available for sampling. □

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## Light speed reduction to 17 metres per second in an ultracold atomic gas

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Techniques that use quantum interference effects are being actively investigated to manipulate the optical properties of quantum systems<sup>1</sup>. One such example is electromagnetically induced transparency, a quantum effect that permits the propagation of light pulses through an otherwise opaque medium<sup>2–5</sup>. Here we report an experimental demonstration of electromagnetically induced transparency in an ultracold gas of sodium atoms, in which the optical pulses propagate at twenty million times slower than the speed of light in a vacuum. The gas is cooled to nanokelvin temperatures by laser and evaporative cooling<sup>6–10</sup>. The quantum interference controlling the optical properties of the medium is set up by a ‘coupling’ laser beam propagating at a right angle to the pulsed ‘probe’ beam. At nanokelvin temperatures, the variation of refractive index with probe frequency can be made very steep. In conjunction with the high atomic density,

this results in the exceptionally low light speeds observed. By cooling the cloud below the transition temperature for Bose–Einstein condensation<sup>11–13</sup> (causing a macroscopic population of alkali atoms in the quantum ground state of the confining potential), we observe even lower pulse propagation velocities ( $17 \text{ m s}^{-1}$ ) owing to the increased atom density. We report an inferred nonlinear refractive index of  $0.18 \text{ cm}^2 \text{ W}^{-1}$  and find that the system shows exceptionally large optical nonlinearities, which are of potential fundamental and technological interest for quantum optics.

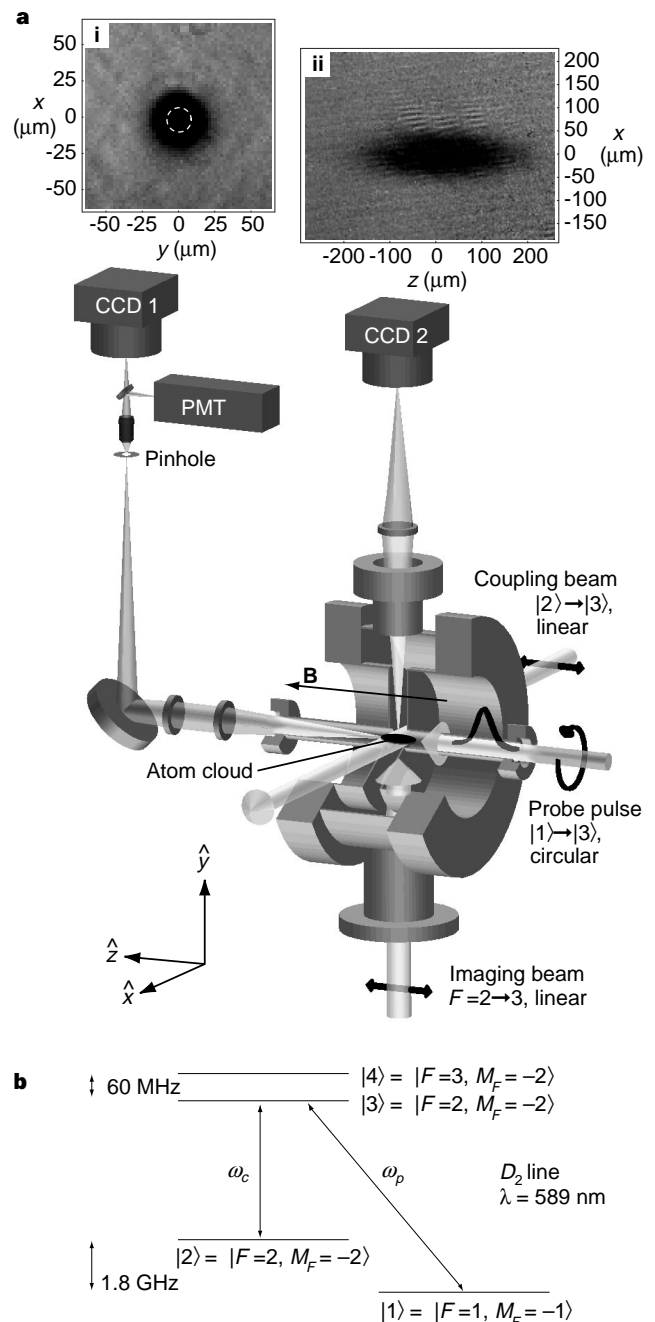
The experiment is performed with a gas of sodium atoms cooled to nanokelvin temperatures. Our atom cooling set-up is described in some detail in ref. 14. Atoms emitted from a ‘candlestick’ atomic beam source<sup>15</sup> are decelerated in a Zeeman slower and loaded into a magneto-optical trap. In a few seconds we collect a cloud of  $10^{10}$  atoms at a temperature of 1 mK and a density of  $6 \times 10^{11} \text{ cm}^{-3}$ . The atoms are then polarization gradient cooled for a few milliseconds to  $50 \mu\text{K}$  and optically pumped into the  $F = 1$  ground state with an equal population of the three magnetic sublevels. We then turn all laser beams off and confine the atoms magnetically in the ‘4 Dee’ trap<sup>14</sup>. Only atoms in the  $M_F = -1$  state, with magnetic dipole moments directed opposite to the magnetic field direction (picked as the quantization axis), are trapped in the asymmetric harmonic trapping potential. This magnetic filtering results in a sample of atoms that are all in a single atomic state (state |1>) in Fig. 1b) which allows adiabatic optical preparation of the atoms, as described below, and minimal heating of the cloud.

Next we evaporatively cool the atoms for 38 s to the transition temperature for Bose–Einstein condensation,  $T_c$ . The magnetic fields are then adjusted to adiabatically soften the trap. The resulting trapping potential has a frequency of  $f_z = 21 \text{ Hz}$  along the symmetry ( $z$ ) axis of the 4 Dee trap, and transverse frequencies  $f_x = f_y = 69 \text{ Hz}$ . The bias field, parallel to the  $z$  axis, is 11 G. When we cool well below  $T_c$ , we are left with 1–2 million atoms in the condensate. For these parameters the transition occurs at a temperature of  $T_c = 435 \text{ nK}$  and a peak density in the cloud of  $5 \times 10^{12} \text{ cm}^{-3}$ .

We now apply a linearly polarized laser beam, the coupling beam, tuned to the transition between the unpopulated hyperfine states |2> and |3> (Fig. 1b). This beam couples states |2> and |3> and creates a quantum interference for a weaker probe laser beam (left circularly polarized) which is tuned to the |1>→|3> transition. A stable eigenstate (the ‘dark state’) of the atom in the presence of coupling and probe lasers is a coherent superposition of the two hyperfine ground states |1> and |2>. The ratio of the probability amplitudes is such that the contributions to the atomic dipole moment induced by the two lasers exactly cancel. The quantum interference occurs in a narrow interval of probe frequencies, with a width determined by the coupling laser power.

Figure 2a shows the calculated transmission of the probe beam as a function of its detuning from resonance for parameters which are typical of this work. In the absence of dephasing of the |1>→|2> transition, the quantum interference would be perfect, and at line centre, the transmission would be unity. Figure 2b shows the refractive index for the probe beam as a function of detuning. Due to the very small Doppler broadening of the |1>→|2> transition in our nanokelvin samples, application of very low coupling intensity leads to a transparency peak with a width much smaller than the natural line width of the |1>→|3> transition. Correspondingly, the dispersion curve is much steeper than can be obtained by any other technique, and this results in the unprecedented low group velocities reported here. The group velocity  $v_g$  for a propagating electromagnetic pulse is<sup>16–19</sup>:

$$v_g = \frac{c}{n(\omega_p) + \omega_p \frac{dn}{d\omega_p}} \approx \frac{\hbar c \epsilon_0 |\Omega_c|^2}{2\omega_p |\mu_{13}|^2 N} \quad (1)$$



**Figure 1** Experimental set-up. A ‘coupling’ laser beam propagates along the  $x$  axis with its linear polarization along the 11-G bias field in the  $z$  direction. The ‘probe’ laser pulse propagates along the  $z$  axis and is left-circularly polarized. With a flipper mirror in front of the camera CCD 1, we direct this probe beam either to the camera or to the photomultiplier (PMT). For pulse delay measurements, we place a pinhole in an external image plane of the imaging optics and select a small area,  $15 \mu\text{m}$  in diameter, of the probe beam centred on the atom clouds (as indicated by the dashed circle in inset (i)). The pulse delays are measured with the PMT. The imaging beam propagating along the  $y$  axis is used to image atom clouds onto camera CCD 2 to find the length of the clouds along the pulse propagation direction ( $z$  axis) for determination of light speeds. Inset (ii) shows atoms cooled to  $450 \text{ nK}$  which is  $15 \text{ nK}$  above  $T_c$ . (Note that this imaging beam is never applied at the same time as the probe pulse and coupling laser). The position of a cloud and its diameter in the two transverse directions,  $x$  and  $y$ , are found with CCD 1. Inset (i) shows an image of a condensate.

Here  $n(\omega_p)$  is the refractive index at probe frequency  $\omega_p$  ( $\text{rad s}^{-1}$ ),  $|\Omega_c|^2$  is the square of the Rabi frequency for the coupling laser and varies linearly with intensity,  $\mu_{13}$  is the electric dipole matrix element between states  $|1\rangle$  and  $|3\rangle$ ,  $N$  is the atomic density, and  $\epsilon_0$  is the permittivity of free space. At line centre, the refractive index is unity, and the second term in the denominator of equation (1) dominates the first. An important characteristic of the refractive index profile is that on resonance the dispersion of the group velocity is zero (see ref. 16), that is,  $d^2n/d\omega_p^2 = 0$ , and to lowest order, the pulse maintains its shape as it propagates. The established quantum interference allows pulse transmission through our atom clouds which would otherwise have transmission coefficients of  $e^{-10}$  (below  $T_c$ ), and creates a steep dispersive profile and very low group velocity for light pulses propagating through the clouds.

We note that the centres of the curves in Fig. 2 are shifted by 0.6 MHz from probe resonance. This is due to a coupling of state  $|2\rangle$  to state  $|4\rangle$  through the coupling laser field, which results in an a.c. Stark shift of level  $|2\rangle$  and a corresponding line shift of the  $2 \rightarrow 3$  transition. As the transparency peak and unity refractive index are obtained at two-photon resonance, this leads to a refractive index at the  $1 \rightarrow 3$  resonance frequency which is different from unity. The difference is proportional to the a.c. Stark shift and hence to the coupling laser intensity, which is important for predicting the nonlinear refractive index as described below.

A diagram of the experiment is shown in Fig. 1a. The 2.5-mm-diameter coupling beam propagates along the  $x$  axis with its linear polarization parallel to the  $\mathbf{B}$  field. The 0.5-mm-diameter,  $\sigma^-$  polarized probe beam propagates along the  $z$  axis. The size and position of the atom cloud in the transverse directions,  $x$  and  $y$ , are obtained by imaging the transmission profile of the probe beam after the cloud onto a charge-coupled-device (CCD) camera. An image of a condensate is shown as inset (i). A  $55 \text{ mW cm}^{-2}$  coupling

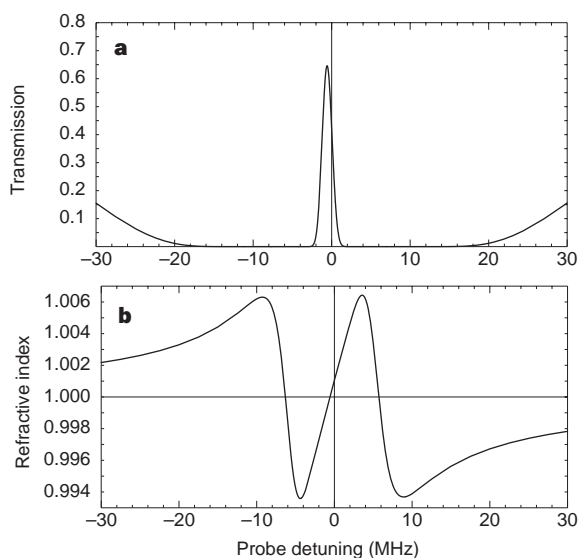
laser beam was present during the 10- $\mu\text{s}$  exposure of the atoms to a  $5 \text{ mW cm}^{-2}$  probe beam tuned close to resonance. The  $f/7$  imaging optics are diffraction-limited to a resolution of  $7 \mu\text{m}$ .

During the pulse delay experiments, a pinhole (placed in an external image plane of the lens system) is used to select only the part of the probe light that has passed through the central  $15 \mu\text{m}$  of the atom cloud where the column density is the greatest. The outline of the pinhole is indicated with the dashed circle in inset (i).

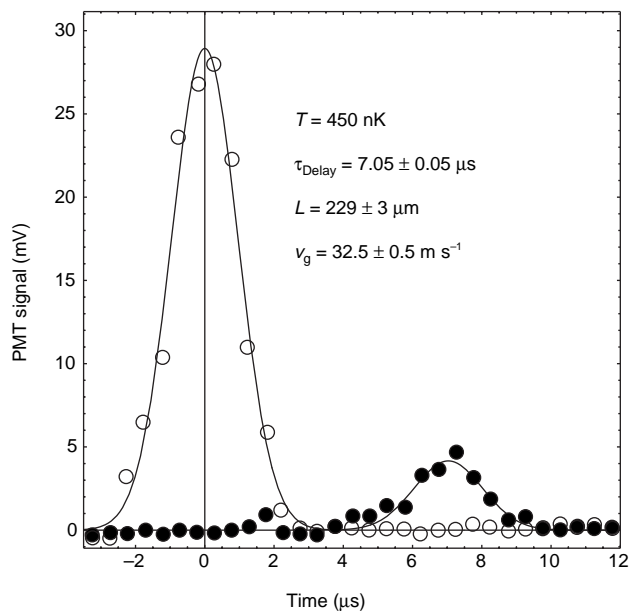
Both coupling and probe beams are derived from the same dye laser. The frequency of the coupling beam is set by an acousto-optic modulator (AOM) to the  $|2\rangle \rightarrow |3\rangle$  resonance. Here we take into account both Zeeman shifts and the a.c. Stark shift described above.

The corresponding probe resonance is found by measuring the transmission of the probe beam as a function of its frequency. We apply a fast frequency sweep, across 32 MHz in 50  $\mu\text{s}$ , and determine resonance from the transmission peak. The sweep is controlled by a separate AOM. The frequency is then fixed at resonance, and the temporal shape of the probe pulse is generated by controlling the r.f. drive power to the AOM. The resulting pulse is approximately gaussian with a full-width at half-maximum of 2.5  $\mu\text{s}$ . The peak power is  $1 \text{ mW cm}^{-2}$  corresponding to a Rabi frequency of  $\Omega_p = 0.20 A$ , where the Einstein  $A$  coefficient is  $6.3 \times 10^7 \text{ rad s}^{-1}$ . To avoid distortion of the pulse, it is made of sufficient duration that its Fourier components are contained within the transparency peak.

Probe pulses are launched along the  $z$  axis 4  $\mu\text{s}$  after the coupling beam is turned on (the coupling field is left on for 100  $\mu\text{s}$ ). Due to the magnetic filtering discussed above, all atoms are initially in state  $|1\rangle$  which is a dark state in the presence of the coupling laser only. When the pulse arrives, the atoms adiabatically evolve so that the probability amplitude of state  $|2\rangle$  is equal to the ratio  $\Omega_p/(\Omega_p^2 + \Omega_c^2)^{1/2}$ , where  $\Omega_p$  is the probe Rabi frequency. To establish the coherent superposition state, energy is transferred from the



**Figure 2** Effect of probe detuning. **a**, Transmission profile. Calculated probe transmission as a function of detuning from the  $|1\rangle \rightarrow |3\rangle$  resonance for an atom cloud cooled to 450 nK, with a peak density of  $3.3 \times 10^{12} \text{ cm}^{-3}$  and a length of  $229 \mu\text{m}$  (corresponding to the cloud in inset (ii) of Fig. 1a). The coupling laser is resonant with the  $|2\rangle \rightarrow |3\rangle$  transition and has a power density of  $52 \text{ mW cm}^{-2}$ . **b**, Refractive index profile. The calculated refractive index is shown as a function of probe detuning for the same parameters as in **a**. The steepness of the slope at resonance is inversely proportional to the group velocity of transmitted light pulses and is controlled by the coupling laser intensity. Note that as a result of the a.c. Stark shift of the  $|2\rangle \rightarrow |3\rangle$  transition, caused by a coupling of states  $|2\rangle$  and  $|4\rangle$  through the coupling laser field, the centre of the transmission and refractive index profiles is shifted by 0.6 MHz. The shift of the refractive index profile results in the nonlinear refractive index described in the text.



**Figure 3** Pulse delay measurement. The front pulse (open circles) is a reference pulse with no atoms in the system. The other pulse (filled circles) is delayed by 7.05  $\mu\text{s}$  in a  $229\text{-}\mu\text{m}$ -long atom cloud (see inset (ii) in Fig. 1a). The corresponding light speed is  $32.5 \text{ m s}^{-1}$ . The curves represent gaussian fits to the measured pulses.

front of the probe pulse to the atoms and the coupling laser field. At the end of the pulse, the atoms adiabatically return to the original state  $|1\rangle$  and the energy returns to the back of the probe pulse with no net energy and momentum transfer to the atomic cloud. Because the refractive index is unity, the electric field is unchanged as the probe pulse enters the medium. As the group velocity is decreased, the total energy density must increase so as to keep constant the power per area. This increase is represented by the energy stored in the atoms and the coupling laser field during pulse propagation through the cloud.

The pulses are recorded with a photomultiplier (3-ns response time) after they penetrate the atom clouds. The output from the photomultiplier is amplified by a 150-MHz-bandwidth amplifier and the waveforms are recorded on a digital scope. With a 'flipper' mirror in front of the camera we control whether the probe beam is directed to the camera or to the photomultiplier.

The result of a pulse delay measurement is shown in Fig. 3. The front pulse is a reference pulse obtained with no atoms present. The pulse delayed by  $7.05\ \mu\text{s}$  was slowed down in an atom cloud with a length of  $229\ \mu\text{m}$  (see Fig. 1a, inset (ii)). The resulting light speed is  $32.5\ \text{m s}^{-1}$ . We used a coupling laser intensity of  $12\ \text{mW cm}^{-2}$  corresponding to a Rabi frequency of  $\Omega_c = 0.56 A$ . The cloud was cooled to  $450\ \text{nK}$  (which is  $15\ \text{nK}$  above  $T_c$ ), the peak density was  $3.3 \times 10^{12}\ \text{cm}^{-3}$ , and the total number of atoms was  $3.8 \times 10^6$ . From these numbers we calculate that the pulse transmission coefficient would be  $e^{-63}$  in the absence of the coupling laser. The probe pulse was indeed observed to be totally absorbed by the atoms when the coupling beam was left off. Inhomogeneous broadening due to spatially varying Zeeman shifts is negligible ( $\sim 20\ \text{kHz}$ ) for the low temperatures and correspondingly small cloud sizes used here.

The size of the atom cloud in the  $z$  direction is obtained with another CCD camera. For this purpose, we use a separate  $1\ \text{mW cm}^{-2}$  laser beam propagating along the vertical  $y$  axis and tuned  $20\ \text{MHz}$  below the  $F = 2 \rightarrow 3$  transition. The atoms are pumped to the

$F = 2$  ground state for  $10\ \mu\text{s}$  before the imaging which is performed with an exposure time of  $10\ \mu\text{s}$ . We image the transmission profile of the laser beam after the atom cloud with diffraction-limited  $f/5$  optics. An example is shown in Fig. 1a, inset (ii), where the asymmetry of the trap is clear from the cloud's elliptical profile. We note that the imaging laser is never applied at the same time as the coupling laser and probe pulse, and for each recorded pulse or CCD picture a new cloud is loaded.

We measured a series of pulse delays and corresponding cloud sizes for atoms cooled to temperatures between  $2.5\ \mu\text{K}$  and  $50\ \text{nK}$ . From these pairs of numbers we obtain the corresponding propagation velocities (Fig. 4). The open circles are for a coupling power of  $52\ \text{mW cm}^{-2}$  ( $\Omega_c = 1.2 A$ ). The light speed is inversely proportional to the atom density (equation (1)) which increases with lower temperatures, with an additional density increase when a condensate is formed. The filled circles are for a coupling power of  $12\ \text{mW cm}^{-2}$ . The lower coupling power is seen to cause a decrease of group velocities in agreement with equation (1). We obtain a light speed of  $17\ \text{m s}^{-1}$  for pulse propagation in an atom cloud initially prepared as an almost pure Bose–Einstein condensate (condensate fraction is  $\geq 90\%$ ). Whether the cloud remains a condensate during and after pulse propagation is an issue that is beyond the scope of this Letter.

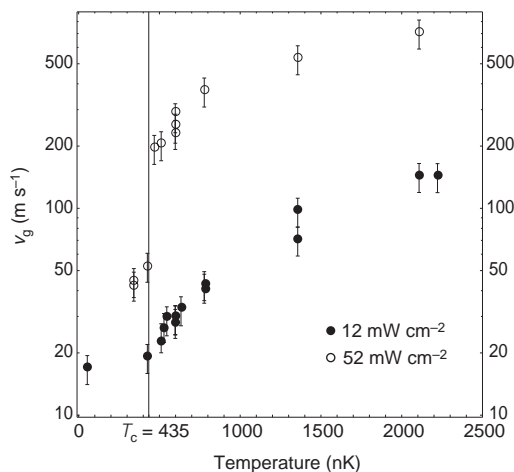
Transitions from state  $|2\rangle$  to state  $|4\rangle$ , induced by the coupling laser (detuned by  $60\ \text{MHz}$  from this transition), result in a finite decay rate of the established coherence between states  $|1\rangle$  and  $|2\rangle$  and limit pulse transmission. The dephasing rate is proportional to the power density of the coupling laser and we expect, and find, that probe pulses have a peak transmission that is independent of coupling intensity and a velocity which reduces linearly with this intensity. The dephasing time is determined from the slope of a semi-log plot of transmission versus pulse delay<sup>19</sup>. At a coupling power of  $12\ \text{mW cm}^{-2}$ , we measured a dephasing time of  $9\ \mu\text{s}$  for atom clouds just above  $T_c$ .

Giant Kerr nonlinearities are of interest for areas of quantum optics such as optical squeezing, quantum nondemolition, and studies of nonlocality. It was recently proposed that they may be obtained using electromagnetically induced transparency<sup>20</sup>. Here we report the first (to our knowledge) measurement of such a nonlinearity. The refractive index for zero probe detuning is given by  $n = 1 + (n_2 I_c)$  where  $I_c$  is the coupling laser intensity, and  $n_2$  the cross phase nonlinear refractive index. As seen from Fig. 2b, the nonlinear term ( $n_2 I_c$ ) equals the product of the slope of the refractive index at probe resonance and the a.c. Stark shift of the  $|2\rangle \rightarrow |3\rangle$  transition caused by the coupling laser. We can then express  $n_2$  by the formula (see equation (1));

$$n_2 = \frac{\Delta\omega_s}{I_c} \frac{dn}{d\omega_p} \approx \frac{1}{2\pi} \frac{\Delta\omega_s \lambda}{I_c v_g} \quad (2)$$

where  $\Delta\omega_s$  is the a.c. Stark shift, proportional to  $I_c$ , and  $\lambda$  the wavelength of the probe transition. We measured an a.c. Stark shift of  $1.3 \times 10^6\ \text{rad s}^{-1}$  for a coupling laser intensity of  $40\ \text{mW cm}^{-2}$ . For a measured group velocity of  $17\ \text{m s}^{-1}$  (Fig. 4), we obtain a nonlinear refractive index of  $0.18\ \text{cm}^2\ \text{W}^{-1}$ . This nonlinear index is  $\sim 10^6$  times greater than that measured in cold Cs atoms<sup>21</sup>.

With a system that avoids the  $|1\rangle$ - $|2\rangle$  dephasing rate described above (which can be obtained by tuning to the  $D_1$  line in sodium), the method used here could be developed to yield the collision-induced dephasing rate of the double condensate which is generated in the process of establishing electromagnetically induced transparency (see also refs 22, 23). In that case, the square of the probability amplitude for state  $|3\rangle$  could be kept below  $10^{-5}$  during pulse propagation, with no heating of the condensate as a result. With improved frequency stability of our set-up and lower coupling intensities, even lower light speeds would be possible, perhaps of the order of centimetres per second, comparable to the speed of



**Figure 4** Light speed versus atom cloud temperature. The speed decreases with temperature due to the atom density increase. The open circles are for a coupling power of  $52\ \text{mW cm}^{-2}$  and the filled circles are for a coupling power of  $12\ \text{mW cm}^{-2}$ . The temperature  $T_c$  marks the transition temperature for Bose–Einstein condensation. The decrease in group velocity below  $T_c$  is due to a density increase of the atom cloud when the condensate is formed. From imaging measurements we obtain a maximum atom density of  $8 \times 10^{13}\ \text{cm}^{-3}$  at a temperature of  $200\ \text{nK}$ . Here, the dense condensate component constitutes  $60\%$  of all atoms, and the total atom density is 16 times larger than the density of a non-condensed cloud at  $T_c$ . The light speed measurement at  $50\ \text{nK}$  is for a cloud with a condensate fraction  $\geq 90\%$ . The finite dephasing rate due to state  $|4\rangle$  does not allow pulse penetration of the most dense clouds. This problem could be overcome by tuning the laser to the  $D_1$  line as described in the text.

sound in a Bose–Einstein condensate. Under these conditions we expect phonon excitation during light pulse propagation through the condensate. By deliberately tuning another laser beam to the  $|2\rangle \rightarrow |4\rangle$  transition, it should be possible to demonstrate optical switching at the single photon level<sup>24</sup>. Finally, we note that during propagation of the atom clouds, light pulses are compressed in the  $z$  direction by a ratio of  $c/v_g$ . For our experimental parameters, that results in pulses with a spatial extent of only 43  $\mu\text{m}$ .  $\square$

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## Luttinger-liquid behaviour in carbon nanotubes

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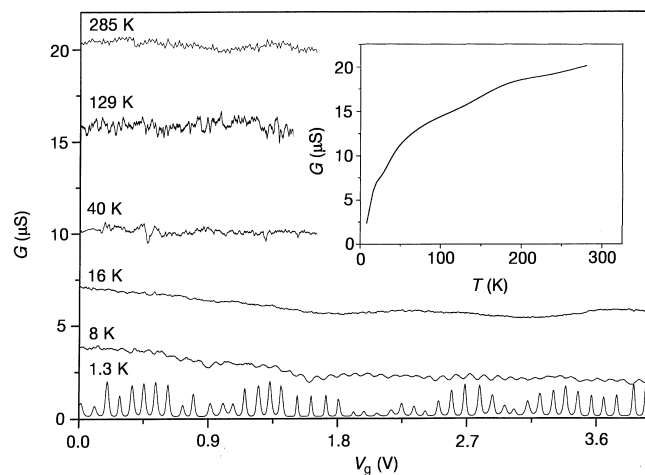
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**Electron transport in conductors is usually well described by Fermi-liquid theory, which assumes that the energy states of the electrons near the Fermi level  $E_F$  are not qualitatively altered by Coulomb interactions. In one-dimensional systems, however, even weak Coulomb interactions cause strong perturbations.**

The resulting system, known as a Luttinger liquid, is predicted to be distinctly different from its two- and three-dimensional counterparts<sup>1</sup>. For example, tunnelling into a Luttinger liquid at energies near the Fermi level is predicted to be strongly suppressed, unlike in two- and three-dimensional metals. Experiments on one-dimensional semiconductor wires<sup>2,3</sup> have been interpreted by using Luttinger-liquid theory, but an unequivocal verification of the theoretical predictions has not yet been obtained. Similarly, the edge excitations seen in fractional quantum Hall conductors are consistent with Luttinger-liquid behaviour<sup>4,5</sup>, but recent experiments failed to confirm the predicted relationship between the electrical properties of the bulk state and those of the edge states<sup>6</sup>. Electrically conducting single-walled carbon nanotubes (SWNTs) represent quantum wires<sup>7–10</sup> that may exhibit Luttinger-liquid behaviour<sup>11,12</sup>. Here we present measurements of the conductance of bundles (‘ropes’) of SWNTs as a function of temperature and voltage that agree with predictions for tunnelling into a Luttinger liquid. In particular, we find that the conductance and differential conductance scale as power laws with respect to temperature and bias voltage, respectively, and that the functional forms and the exponents are in good agreement with theoretical predictions.

SWNTs are sufficiently robust and long to allow electrical connections to lithographically defined metallic electrodes, thereby making it possible to probe the intriguing electrical properties of



**Figure 1** The two-terminal linear-response conductance  $G$  versus gate voltage  $V_g$  for a bulk-contacted metallic nanotube rope at a variety of temperatures. The data show significant temperature dependence for energy scales above the charging energy that cannot be explained by the Coulomb blockade model. Inset: average conductance as a function of temperature  $T$ . The samples used in these experiments are made in one of two ways. In both methods, SWNTs are deposited from a suspension in dichloroethane onto a 1- $\mu\text{m}$ -thick layer of  $\text{SiO}_2$  that has been thermally grown on a degenerately doped Si wafer, used as a gate electrode. Atomic force microscopy imaging reveals that the diameters of the ropes vary between 1 and 10 nm. In the first method<sup>9</sup>, chromium-gold contacts are applied over the top of the nanotube rope using electron beam lithography and lift-off. From measurements of these devices in the Coulomb blockade regime, we conclude that the electrons are confined to the length of rope between the leads. This implies that the leads cut the nanotubes into segments, and transport involves tunnelling into the ends of the nanotubes (‘end-contacted’). In the second method<sup>10</sup>, electron-beam lithography is first used to define leads, and ropes are deposited on top of the leads. Samples were selected that showed Coulomb blockade behaviour at low temperatures with a single well-defined period, indicating the presence of a single quantum dot. The charging energy of these samples indicates a quantum dot with a size substantially larger than the spacing between the leads, as found by Tans *et al.*<sup>10</sup>. Transport thus occurs by electrons tunnelling into the middle, or bulk, of the nanotubes (‘bulk-contacted’).